

L#7

# Basics of Programming. Procedures and functions

Course Basics of Programming Semester 1, FIIT

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# + and \* operations for arrays

**a + b** – concatenation of two arrays into result array

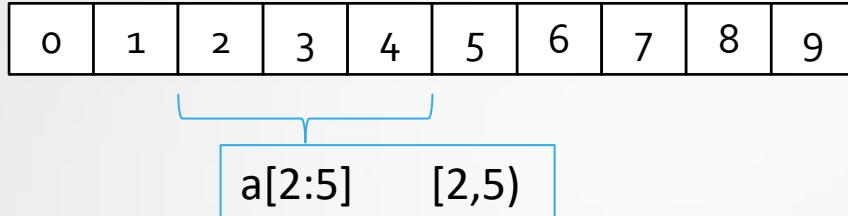
**a \* N** – concatenation of **N** copies of **a** into result array

```
var a := Arr(1,2,3);
var b := Arr(4,5,6);

a + b // 1 2 3 4 5 6
a * 3 // 1 2 3 1 2 3 1 2 3
Arr(1) * 10 // 1 1 1 1 1 1 1 1 1 1
Arr(1)*5 + Arr(2)*5 // 1 1 1 1 1 2 2 2 2 2
(Arr(1) + Arr(2))*5 // 1 2 1 2 1 2 1 2 1 2
```

# Array slices

```
var a := Arr(0,1,2,3,4,5,6,7,8,9);
```



**Array slice** is a subarray of original array

It has one of two forms: **a[x:y]** or **a[x:y:step]**. Expressions **x** and **y** can be omitted.

<b>a[:4]</b>	- 0 1 2 3
<b>a[4:]</b>	- 4 5 6 7 8 9
<b>a[:a.Length-1]</b>	- 0 1 2 3 4 5 6 7 8
<b>a[:]</b>	- 0 1 2 3 4 5 6 7 8 9 (copy of a)
<b>a[::-2]</b>	- 0 2 4 6 8
<b>a[1::2]</b>	- 1 3 5 7 9
<b>a[4:1:-1]</b>	- 4 3 2
<b>a[::-1]</b>	- 9 8 7 6 5 4 3 2 1 0 (reverse of a)

# Example

- **To do:** an array  $A$  of size  $N$  and an integer  $K$  ( $1 \leq K \leq N$ ) are given. Print its elements with ordinal numbers (i.e. indexes) that are multiples of  $K$  (i.e. divisible by  $K$ ):
  - $A_k, A_{2 \cdot k}, A_{3 \cdot k} \dots$
  - Do not use the `if` statement.

```
begin
var n:=ReadInteger('how many elements'); // 4
var a:=ReadArrReal(n); // 2 6 7 5
var k:=ReadInteger('K='); // 2
a[k-1 : : k].Print; // 6 5
end.
```

# Example

- **To do:** An array **A** of size **N** is given. First, output its elements with even ordinal numbers (in ascending order of ordinal numbers), and then — elements with odd ordinal numbers (also in ascending order of ordinal numbers):

$a_2, a_4, a_6, \dots a_1, a_3, a_5 \dots$

- Do not use conditional operator.

```
begin
var n:=ReadInteger('how many elements');
var a:=arrRandomInteger(n);
a.Println;
var slice:=a[1::2]+a[::2];
slice.Print
end.
```

```
how many elements 10
8 96 24 61 80 60 24 40 95 15
96 61 60 40 15 8 24 80 24 95
```

# Example

- **To do:** An array of size **N** and integers **K** and **L** ( $1 \leq K \leq L \leq N$ ) are given. Find the arithmetic mean (average) of the elements of an array with numbers from **K** to **L** inclusive.

```
begin
var n:=ReadInteger;
var a:=arrrandominteger(n);
a.Println;
var k:=ReadInteger('K = ');
var l:=ReadInteger('L = ');
var slice:=a[k-1:l].Average;
slice.Print;
end.
```

```
>> 10
59 87 0 37 57 69 79 19 100 5
K = >> 2
L = >> 4
41.33333333333333
```

# Example

- **To do:** An array of size **N** is given. Find the minimum element of its even-numbered elements:

$a_2, a_4, a_6, \dots$

```
begin
var n:=ReadInteger;
var a:=arrRandomInteger(n);
a.Println;
println('slice: ', a[1::2]);
print(a[1::2].min);
end.
```

```
>> 10
96 79 71 87 61 21 51 74 67 89
slice: [79,87,21,74,89]
21
```

# Reverse of an array

```
begin
var a:=new integer[10];
a:=arrRandomInteger(10);
print(a); // [41,81,84,63,12,26,88,25,36,72]
Reverse(a);
print(a) // [72,36,25,88,26,12,63,84,81,41]
end.
```

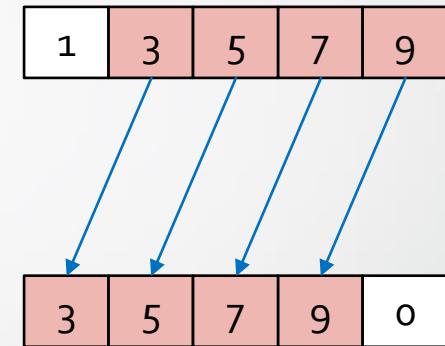
A standard **Reverse(a)** procedure has this algorithm. Thus, we don't need to create it in our program, it's possible just to use it.

We can use slices: `a := a[::-1]`

# Shift to the left

**Problem:** Create a user procedure to shift the elements to the left

```
procedure ShiftLeft<T>(a: array of T);  
begin  
    for var i := 0 to a.Length - 2 do  
        a[i] := a[i + 1];  
    a[a.Length - 1] := default(T);  
end;  
  
begin  
    var a := new integer[5];  
    a := arrRandomInteger(5); // [56,28,33,57,25]  
    shiftLeft(a);  
    print(a) // [28,33,57,25,0]  
end.
```

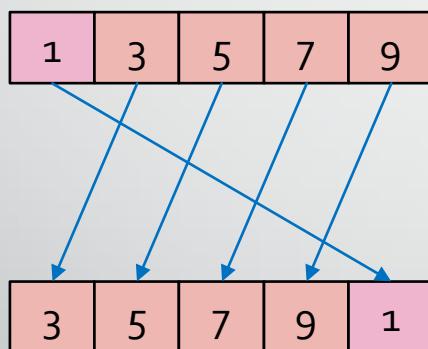


With slices:  
a := a[1:] + Arr(0);

[3, 5, 7, 9] + [0]

# Circular shift left

```
procedure CircularShiftLeft<T>(a: array of T);  
begin  
    var v := a[0];  
    for var i:=0 to a.Length-2 do  
        a[i] := a[i+1];  
    a[a.Length-1] := v;  
end;
```

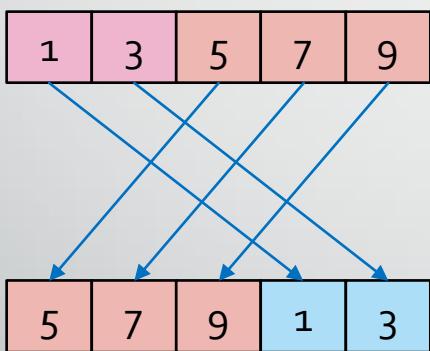


With slices:  
 $a := a[1:] + a[:1];$

$[3, 5, 7, 9] + [1]$

# Circular shift left by k

1. **loop** k do  
    CircularShiftLeft(a); // ineffective
2. With second array
3. With partial reverse



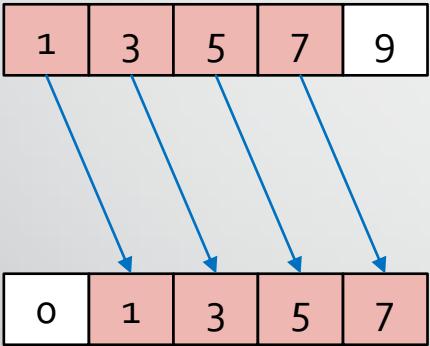
$k = 2$

Using slices:  
 $a := a[k:] + a[:k];$

$[5, 7, 9] + [1, 3]$

# Shift right

```
procedure ShiftRight<T>(a: array of T);  
begin  
    for var i:=a.Length-1 downto 1 do  
        a[i] := a[i-1];  
    a[0] := default(T);  
end;
```



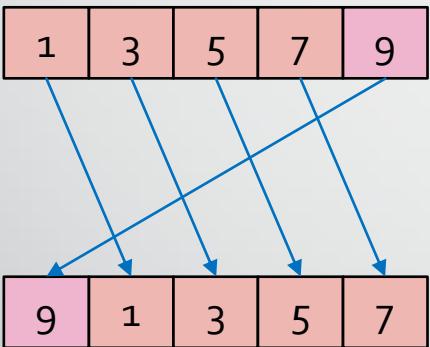
Using slices:

$a := \text{Arr}(0) + a[:a.Length-1];$

$[0] + [1, 3, 5, 7]$

# Circular shift to the right

```
procedure CircularShiftRight<T>(a: array of T);  
begin  
    var v := a[a.Length-1];  
    for var i:=a.Length-1 downto 1 do  
        a[i] := a[i-1];  
    a[0] := v;  
end;
```



Using slices:

```
var m := a.Length-1;  
a := a[m:] + a[:m];
```

[9] + [1, 3, 5, 7]

# Insertion and deletion in an array using slices

**Problem 1.** An array of **N** integers is given. It's necessary to insert an element **x** on **k**-th index, **k<=N**.

```
begin
  var a := arr(5, 12, 1, 3, 11, 19);
  var x := ReadInteger ('enter a number to insert');
  var k := ReadInteger ('enter an order number');
  a := a[:k] + Arr(x) + a[k:];
  print(a) // [5,12,3,1,3,11,19]
end.
```

**Problem 2.** An array of **N** integers is given. It's necessary to delete an element with index **k**, **k<N**.

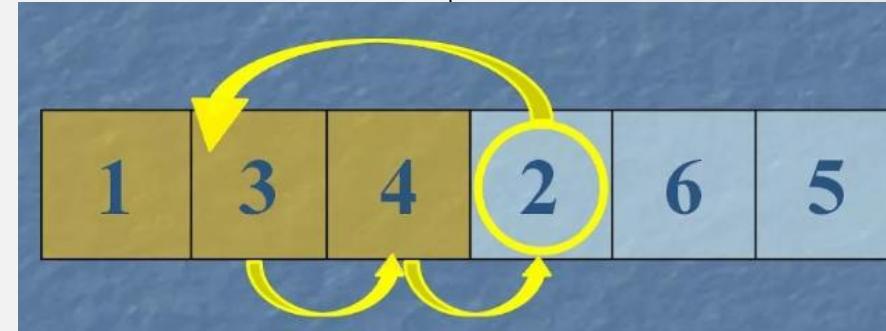
```
begin
  var a := arr(5, 12, 1, 3, 11, 19);
  var k := ReadInteger ('enter an order number');
  a := a[:k] + a[k+1:];
  print(a) // [5,12,3,11,19]
end.
```

- Tasks 1,2,3,4,5,6,7,8

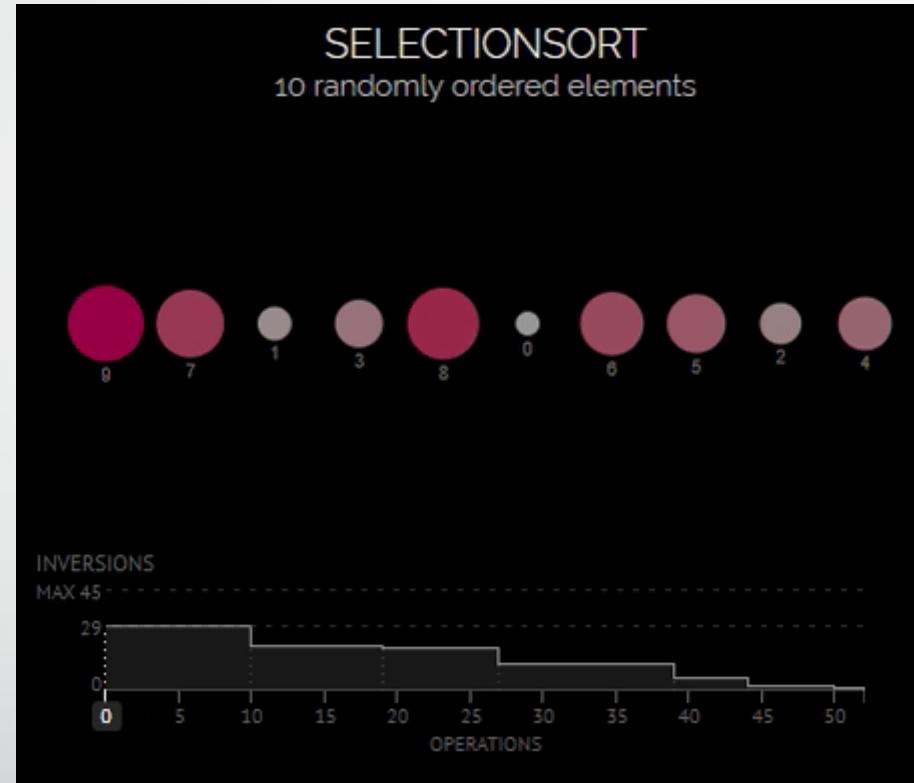
# Array sorting algorithms

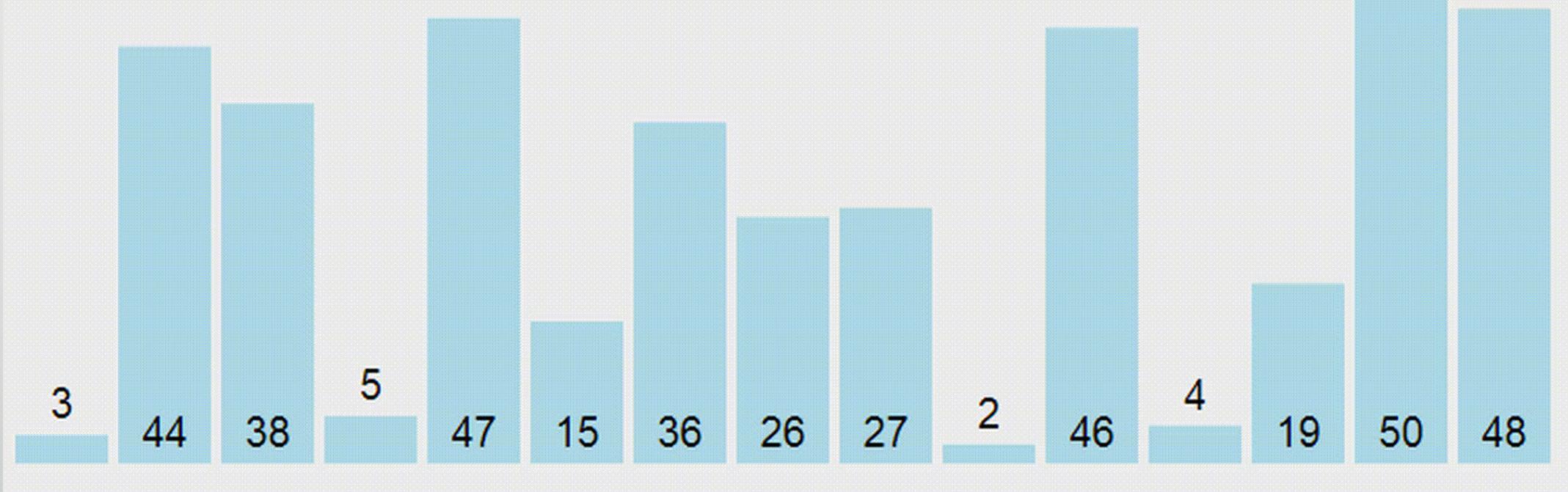
# Selection sort

```
procedure SelectionSort(a: array of integer);  
begin  
    for var i := 0 to a.High-1 do  
        begin  
            var (min,imin) := (a[i],i);  
            for var j := i + 1 to a.High do  
                if a[j] < min then  
                    (min,imin) := (a[j],j);  
                Swap(a[imin],a[i]);  
        end;  
    end;
```



- this algorithm iterates over the array over and over, moving one value to the correct position
- At the next iteration, we will find the minimum in the array after the current element and change it with it, if necessary. Thus, after the  $i$ -th iteration, the first  $i$  elements will stay in their places.
- it selects the smallest unsorted value and swap it with that which was the smallest
- the sorted portion of the array is at the beginning





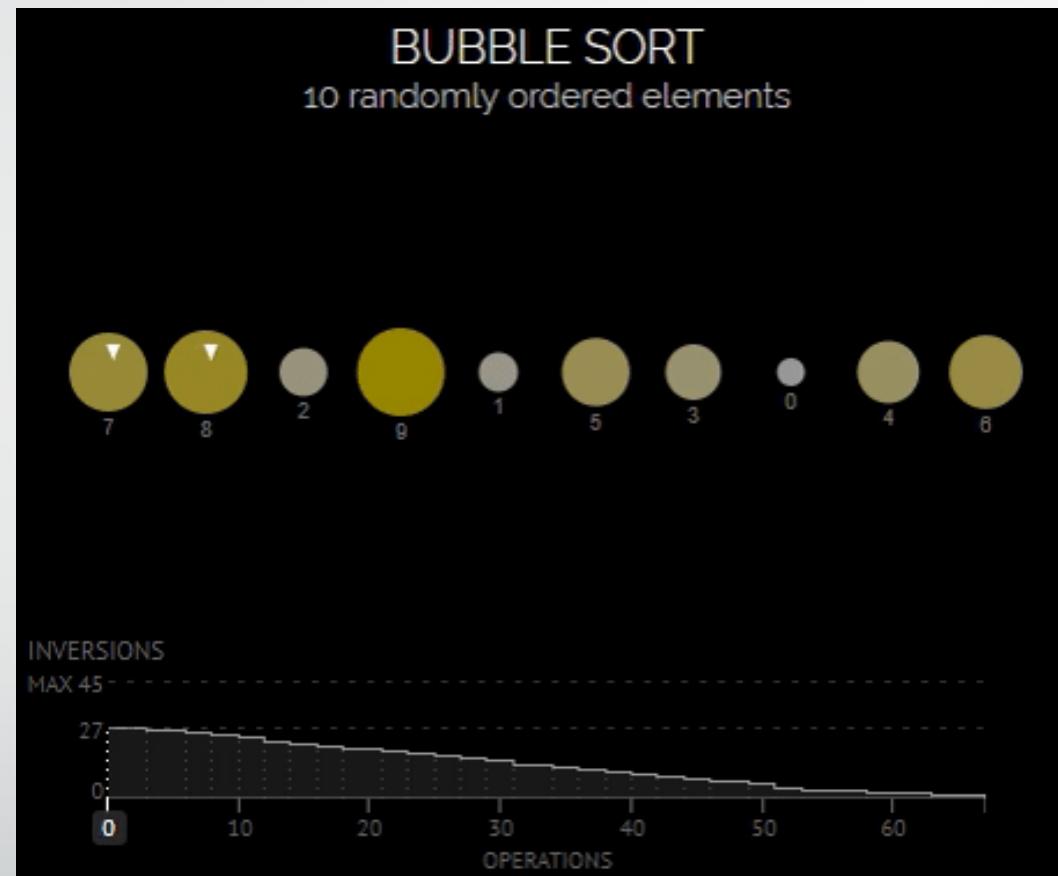
```
procedure SelectionSort(a: array of integer);
begin
  for var i := 0 to a.High-1 do
    begin
      var (min,imin) := (a[i],i);
      for var j := i + 1 to a.High do
        if a[j] < min then
          (min,imin) := (a[j],j);
      Swap(a[imin],a[i]);
    end;
end;
```

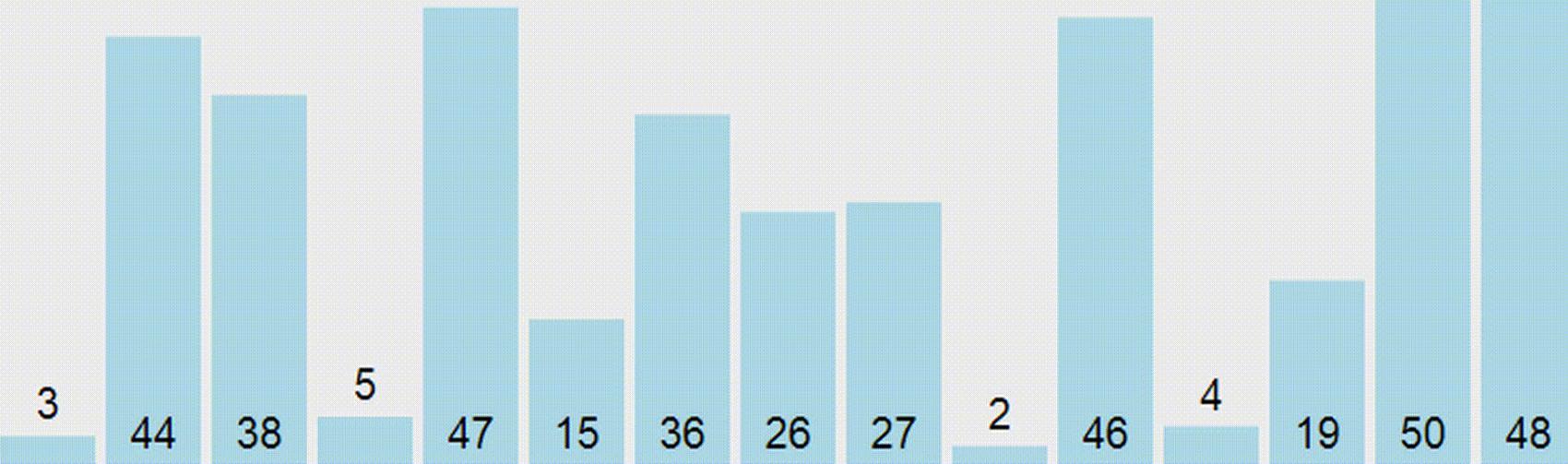
# Bubble sort

```
procedure BubbleSort(arr: array of integer);  
begin  
    for var i := 1 to arr.High - 1 do  
        for var j := 0 to arr.High - i do  
            if arr[j] > arr[j + 1] then  
                Swap(arr[j], arr[j + 1]);  
end;
```

	6 > 1, swap
	6 > 2, swap
	6 > 3, swap
	6 > 4, swap
	6 > 5, swap
	1 < 2, ok
	2 < 3, ok
	3 < 4, ok
	4 < 5, ok

- Let's iterate over the array from left to right.
- If the current element is greater than the next one, we swap them.
- We do this until the array is sorted.
- Note that after the first iteration, the largest element will be at the end of the array, in the correct place.
- After two iterations, the two largest items will be in the correct place, and so on.





```
procedure BubbleSort(arr: array of
integer);
begin
  for var i := 1 to arr.High - 1 do
    for var j := 0 to arr.High - i do
      if arr[j] > arr[j + 1] then
        Swap(arr[j], arr[j + 1]);
  end;
```

# Bubble sort 2

```
procedure BubbleSort2(a: array of integer);  
begin  
    var i := a.High;  
    var q: boolean;  
    repeat  
        q := true;  
        for var j := 0 to i - 1 do  
            if a[j+1] < a[j] then  
                begin  
                    Swap(a[j+1], a[j]);  
                    q := false;  
                end;  
        i -= 1;  
    until q;  
end;
```

# Insertion sort

```
procedure SortByInsert(a: array of integer);
begin
  for var i:=1 to a.High do
    begin
      var x := a[i];
      var j := i - 1;
      while (j >= 0) and (x < a[j]) do
        begin
          a[j+1] := a[j];
          j -= 1;
        end;
      a[j+1] := x;
    end;
end;
```

After insertion of every element we have sorted array.

X is a variable to store the value while comparing others

The *Insertion sort* algorithm iterates through the elements of the array one at a time, and places each new taken element in a suitable place among the previously ordered elements.

14	13	11	0	19	13
----	----	----	---	----	----

14 храним «в уме» и сравниваем

1

14	14	11	0	19	13
----	----	----	---	----	----

13	14	11	0	19	13
----	----	----	---	----	----

13	14	11	0	19	13
----	----	----	---	----	----

11 храним «в уме»

13	14	14	0	19	13
----	----	----	---	----	----

13	13	14	0	19	13
----	----	----	---	----	----

11	13	14	0	19	13
----	----	----	---	----	----

0 храним «в уме» и сравниваем

11	13	14	0	19	13
----	----	----	---	----	----

11	13	13	14	19	13
----	----	----	----	----	----

11	13	13	14	19	13
----	----	----	----	----	----

0	11	13	14	19	13
---	----	----	----	----	----

0	11	13	14	19	13
---	----	----	----	----	----

19 храним «в уме» и сравниваем

4

0	11	13	14	19	13
---	----	----	----	----	----

0	11	13	14	19	13
---	----	----	----	----	----

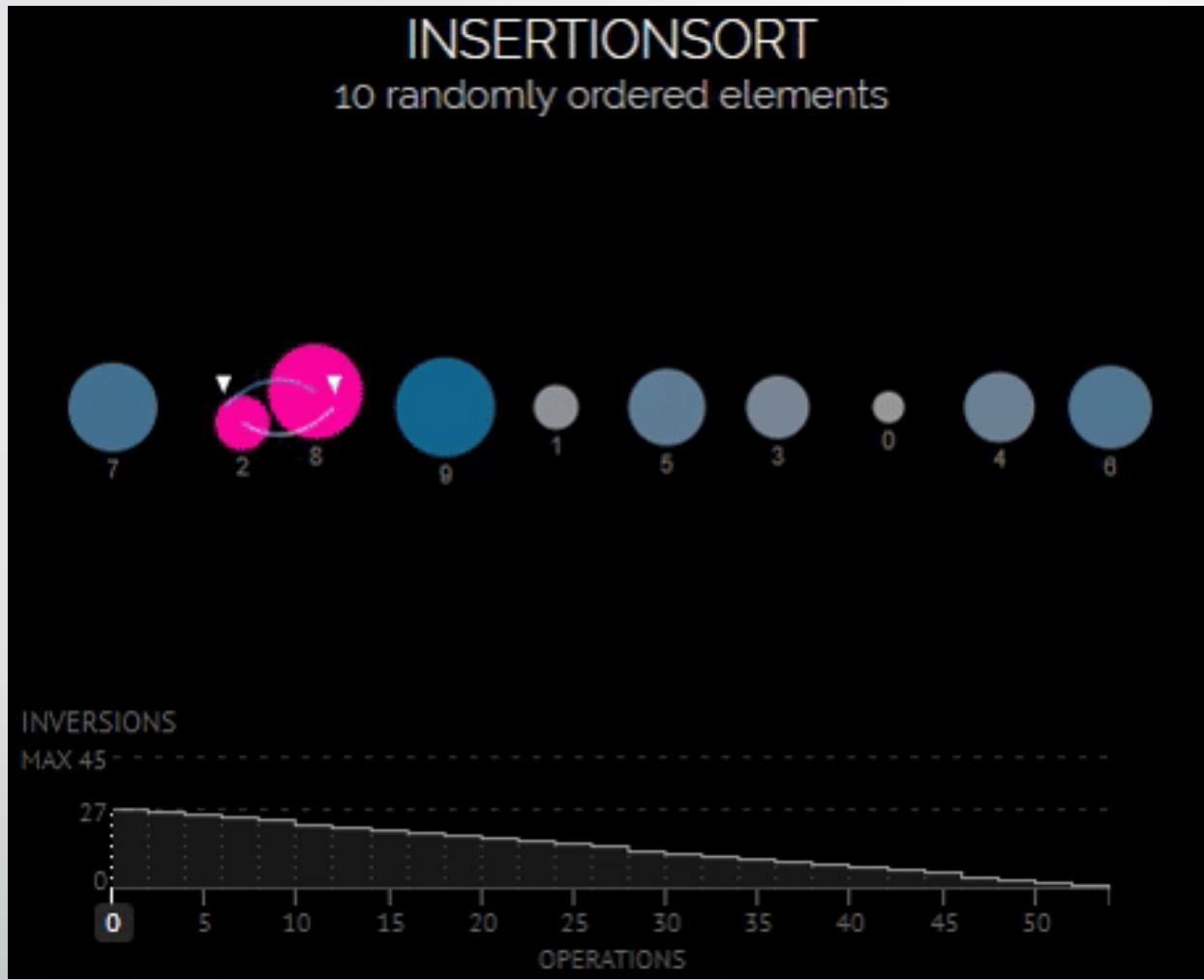
13 храним «в уме» и сравниваем

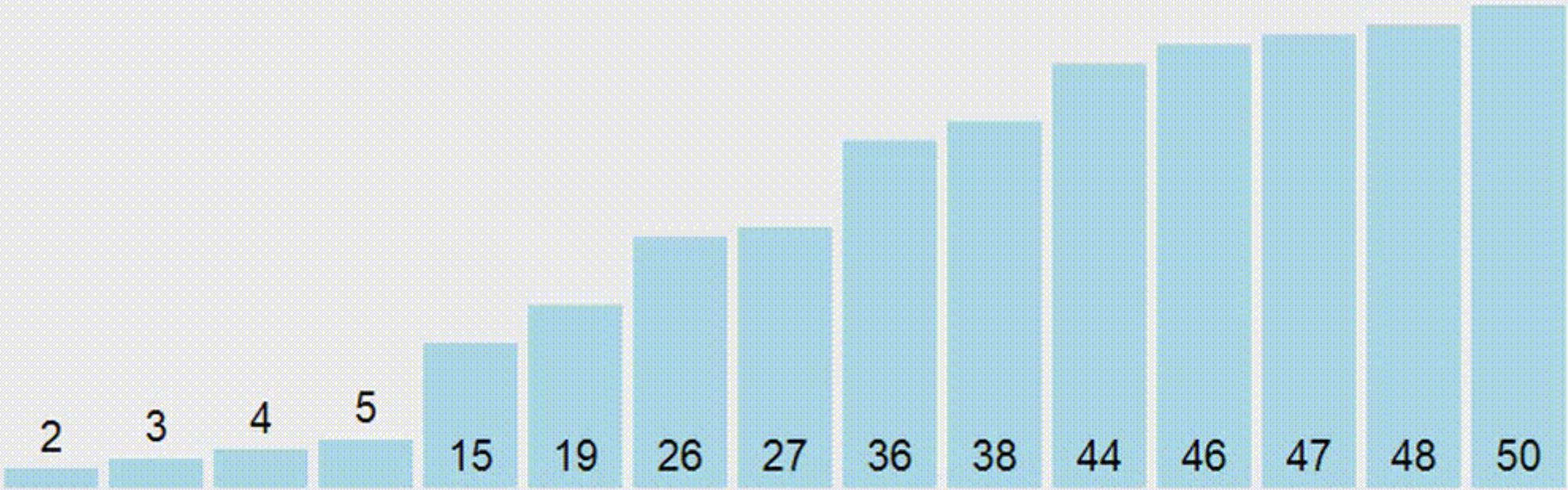
0	11	13	14	19	19
---	----	----	----	----	----

0	11	13	14	14	19
---	----	----	----	----	----

0	11	13	13	14	19
---	----	----	----	----	----

Пока меньше выполняем ...





```
procedure SortByInsert(a: array of integer);
begin
  for var i:=1 to a.High do
  begin
    var x := a[i];
    var j := i - 1;
    while (j >= 0) and (x < a[j]) do
    begin
      a[j+1] := a[j];
      j -= 1;
    end;
    a[j+1] := x;
  end;
end;
```

# Standard sort

```
Sort(a);
```

```
SortByDescending(a);
```

# Program execution time

- **To do:** calculate a time to execute the algorithm of Bubble sort

```
procedure MySort(a: array of integer);
begin
// bubble sort
  for var i := 0 to a.High-1 do
    for var j := a.High downto i+1 do
      if a[j] < a[j-1] then
        Swap(a[j], a[j-1]);
end;
begin
var a:=arrRandomInteger(20000);
// note the time
var t:=System.DateTime.Now;
// run the algorithm
MySort(a);
// note the time of algorithm end
var t1:=System.DateTime.Now;
writeln('The time to execite the algorithm: ',t1-t);
//t:=System.DateTime.Now;
end.
```

- Task 9

# Merging of two sorted arrays

# Merging of two sorted arrays

**Problem.** Two sorted arrays **a** and **b** are given.

Merge them into third sorted array

**Solution (bad):**

```
var c := a + b;  
Sort(c);
```

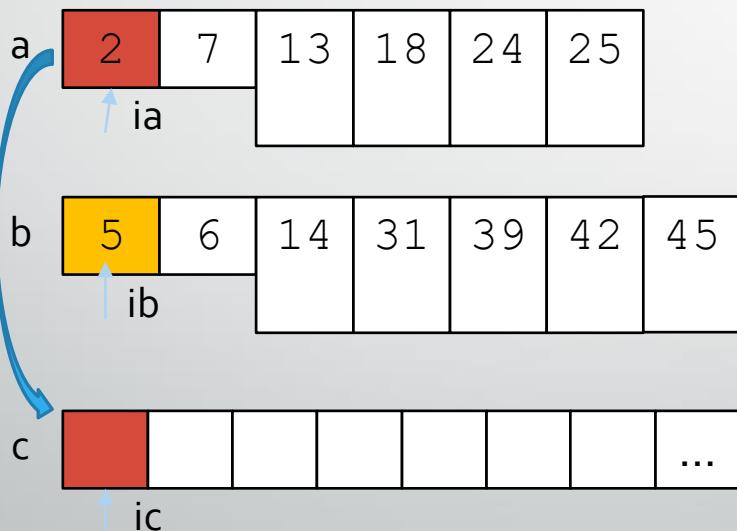
```
begin  
  var a:=arr(1,3,11,19);  
  var b:=arr(1,13,21);  
  var c:=a+b; // [1,3,11,19,1,13,21]  
  Sort(c); // [1,1,3,11,13,19,21]  
end.
```

# Merging of two sorted arrays

**Problem.** Two sorted arrays **a** and **b** are given.

Merge them into third sorted array

**Solution** (partial). Let's use the counter **ia** as an index of the first element of **a** and counter **ib** – as the index of the first element of **b**. If **a[ia]<b[ib]**, then copy **a[ia]** to **c** and increase **ia**. Else copy **b[ib]** and increase **ib**.

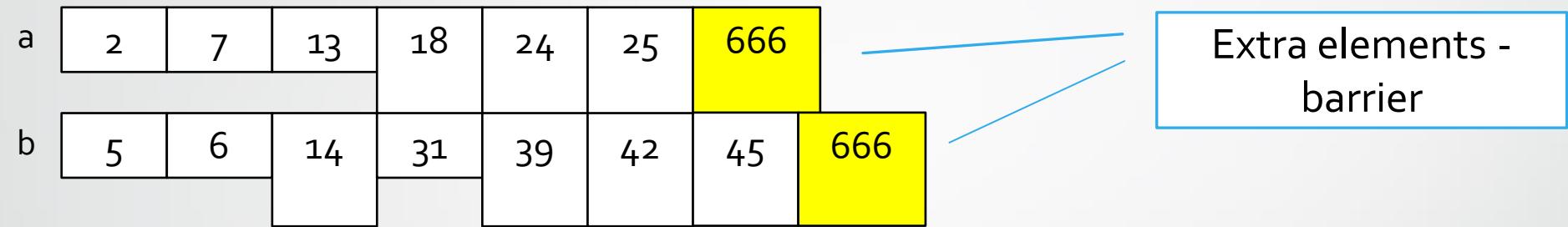


It doesn't work! Why?

```
var (ia,ib) := (0,0);
for var ic:=0 to c.Length-1 do
  if a[ia]<b[ib] then
    begin
      c[ic] := a[ia];
      ia += 1
    end
  else
    begin
      c[ic] := b[ib];
      ib += 1
    end;
```

# Merging of two sorted arrays

**Solution (complete).** Let's add the barrier element to the end of every array^



Previous code will work correctly!

# Merging of two sorted arrays

```
function Merge(a, b: array of integer; n, m: integer): array of real;  
begin  
    Assert((0 < n) and (n < a.Length));  
    Assert((0 < m) and (m < b.Length));  
    a[n] := integer.MaxValue; // barrier  
    b[m] := integer.MaxValue; // barrier  
    SetLength(Result, m + n);  
    var (ia, ib) := (0, 0);  
    for var ic := 0 to n + m - 1 do  
        if a[ia] < b[ib] then  
            begin  
                Result[ic] := a[ia];  
                ia += 1;  
            end  
        else  
            begin  
                Result[ic] := b[ib];  
                ib += 1;  
            end;  
    end;
```

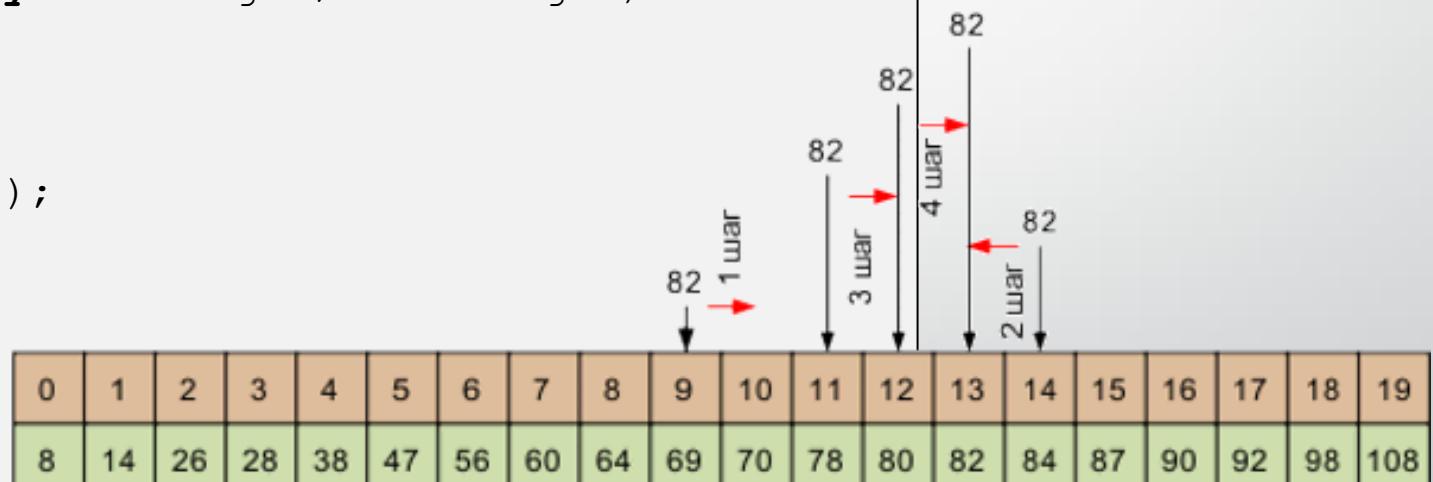
```
begin  
    var a := arr(1, 3, 11, 19);  
    var b := arr(1, 13, 21);  
    setLength(a, 5); // for extra element  
    setLength(b, 4); // for extra element  
    print(Merge(a, b, 4, 3)) // [1,1,3,11,13,19,21]  
end.
```

# Binary search in a sorted array

## Standard method **a.BinarySearch(x)**

Code of the method (не рассматривать).

```
function BinarySearch(a: array of integer; x: integer):  
integer;  
begin  
  var k: integer;  
  var (l, r) := (0, a.Length-1);  
  repeat  
    k := (l+r) div 2;  
    if x>a[k] then  
      l := k+1  
    else r := k-1;  
  until (a[k]=x) or (l>r);  
  Result := a[k]=x ? k : -1;  
end;
```



- Task 10, 11

List

# List<T>

**List** is a kind of dynamic array with dynamic change of its size during program execution.

**List definition:**

real, array of integer, ...

```
var l := new List<integer>; // l.Count = 0
```

**Short definition with initialization:**

```
var L := Lst(25, -23, 47, 100, 0, 14);
```

Or:

```
var L2 := Lst(Arr(14, 172, -5, 0, 39)); // [14,172,-5,0,39]
var L3 := Lst(ArrRandom(5, -99, 99)); // [0,-6,2,-81,10]
var L4 := Lst(L3); // there is one element there in L4 list,
it is list [[0,-6,2,-81,10]]
```

# List<T>

**Adding** an element to the end of a list:

```
var L := Lst(Arr(14, 172, -5, 0, 39));
L.Add(5); // List is expanded
L.Add(3);
L.Add(4);
L += 8; // a synonym of l.Add(8)
println(L); // [14,172,-5,0,39,5,3,4,8]
```

**Iterating over the list:**

```
for var i:=0 to L.Count-1 do
    Print(L[i]);
foreach var x in L do
    Print(x);
```

# List operations and methods

Operations with list:

```
var L := Lst(5,2,3);
Print(2 in L); // True
Print(2 * L); // [5,2,3,5,2,3]
L.Print; // 5 2 3
Print(L + Lst(7,6,8)); // 5 2 3 7 6 8
```

Methods of list:

```
L.Insert(ind,x); // insert x by index ind
L.RemoveAt(ind); // delete element by index ind
L.RemoveRange(ind,count) // delete a diapason of elements
L.RemoveAll(x -> x.IsOdd); // delete elements by condition
L.IndexOf(3); // index of a first element or -1
L.FindIndex(x -> x > 4); // index of a first element or -1
L.Clear;
L.Reverse;
L.Sort;
```

# Examples

**Problem.** An array of **N** integers is given. Insert all even elements of the array into **L1**, and all odd elements into **L2**

**Solution.**

```
begin
    var a := arrrandominteger(10, 5, 25);
    println(a); // [17,25,8,17,21,9,19,22,19,24]
    var L1 := new List<integer>;
    var L2 := new List<integer>;

    foreach var x in a do
        if x.Iseven then
            L1 += x
        else L2 += x;
    L1.println; // 8 22 24
    L2.println; // 17 25 17 21 9 19 19
end.
```

# Insertion and deletion in an array using lists methods

**Problem 1.** An array of **N** integers is given. It's necessary to insert an element **x** on **k**-th index, **k<=N**.

```
begin
    var a := arr(5, 12, 1, 3, 11, 19);
    var x := ReadInteger ('enter a number to insert');
    var k := ReadInteger ('enter an order number');
    a := a[:k] + Arr(x) + a[k:];
    print(a) // [5,12,3,1,3,11,19]
end.
```

**With lists:**  
**L.Insert(k,x);**

**Problem 2.** An array of **N** integers is given. It's necessary to delete an element with index **k**, **k<N**.

```
begin
    var a := arr(5, 12, 1, 3, 11, 19);
    var k := ReadInteger ('enter an order number');
    a := a[:k] + a[k+1:];
    print(a) // [5,12,3,11,19]
end.
```

**With lists:**  
**L.RemoveAt(k);**

- Task 12, 13, 14

# Q & A